PARUL UNIVERSITY
FACULTY OF ENGINEERING \& TECHNOLOGY
M.Tech., Winter 2017-18 Examination

Semester: 1
Subject Code: 03218101
Subject Name: Design And Analysis of Experiments

Date: 28/12/2017
Time: 2:00pm to 4:30pm
Total Marks: 60

## Instructions:

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Make suitable assumptions wherever necessary.
4. Start new question on new page.
Q. 1 A) Compute the student $t$ for the following value in a sample of eight.

$$
2,4,6,7,7,8,8,9
$$

Taking the mean of universe to be zero.
B) Result of throwing die were recorded as follows:

| Number Turned up | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 27 | 33 | 31 | 29 | 30 | 24 |

Is the die biased?
C) Calculate coefficient of correlation between x and y using following data.

| X | 2 | 4 | 5 | 6 | 8 | 11 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 18 | 12 | 10 | 8 | 7 | 5 |

Q. 2 Answer the following questions. (Attempt any three)
A) Ten young recruits were put through a strenuous physical training program by the army. Their weights (in kg ) were recorded before and after with the following results:

| Recruit | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Weight <br> before | 127 | 195 | 162 | 170 | 143 | 205 | 168 | 175 | 197 | 136 |
| Weight <br> after | 135 | 200 | 160 | 182 | 147 | 200 | 172 | 186 | 194 | 141 |

Using 5\% level of significance, should we conclude that the program affects the average weight of young recruits (Answer using t -test).
B) Answer using F-test whether the following two samples have come from the same population:

| Sample 1 | 20 | 25 | 28 | 24 | 19 | 26 | 21 | 22 | 23 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sample 2 | 19 | 18 | 21 | 22 | 24 | 17 | 20 | 18 |  |

Use 5\% of Significance.
C) Raju Restaurant near the railway station at Falna has been having average sales of 500 tea cups per day. Because of the development of bus stand nearby, it expects to increase its sales. During the first 12 days after the start of the bus stand, the daily sales were as under:

$$
550,570,490,615,505,580,570,460,600,580,530,526
$$

On the basis of this sample information, can one conclude that Raju Restaurant's sales have increased? Use 5 per cent level of significance.
D) The following table gives the number of units produced per day by two workers A and B for a number of days:

| A | 40 | 30 | 38 | 41 | 38 | 35 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| B | 39 | 38 | 41 | 33 | 32 | 49 | 49 | 34 |

Should these results be accepted as evidence that B is the more stable worker? Use F-test at 5\% level.
Q. 3 A) Set up an ANOVA Table for the following per acre production data for three varieties of wheat, each grown on 4 plots and state if the variety difference is significant. (BY DIRECT METHOD)

| Plot of land | Per acre production data |  |  |
| :--- | :--- | :--- | :--- |
|  | Variety of wheat |  |  |
|  | A | B | C |
| 1 | 6 | 5 | 5 |
| 2 | 7 | 5 | 4 |
| 3 | 3 | 3 | 3 |
| 4 | 8 | $`$ | 4 |

Q. 3 B) Analyze and interpret the following statistics concerning output of wheat per field obtained as a result of experiment conducted to test four varieties of wheat viz., $A, B, C$ and $D$ under a Latin square design.

| C | B | A | D |
| :---: | :---: | :---: | :---: |
| 25 | 23 | 20 | 20 |
| A | D | C | B |
| 19 | 19 | 21 | 18 |
| B | A | D | C |
| 19 | 14 | 17 | 20 |
| D | C | B | A |
| 17 | 20 | 21 | 15 |

Q. 3 B) Present your conclusions after doing analysis of variance to the following results of the Latinsquare design experiment conducted in respect of five fertilizers which were used on plots of different fertility.

| A | D | C | B |
| :---: | :---: | :---: | :---: |
| 26 | 24 | 24 | 20 |
| C | B | A | D |
| 20 | 24 | 22 | 18 |
| D | C | B | A |
| 16 | 18 | 20 | 22 |
| B | A | D | C |
| 22 | 20 | 18 | 16 |

Q. 4 A) Obtain two regression lines from the following data and hence find the correlation of coefficient.

| $x$ | 6 | 2 | 10 | 4 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | 9 | 11 | 5 | 8 | 7 |

## OR

Q. 4 A) The participants in contest are ranked by two judges as follows:

| x | 1 | 3 | 7 | 5 | 4 | 6 | 2 | 10 | 9 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| y | 3 | 1 | 4 | 5 | 6 | 9 | 7 | 8 | 10 | 2 |

Q. 4 B) The following are the no. of defective blocks produced by the 4 workers operating on three different machines.

| MACHINES | workers |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
| M1 | 37 | 38 | 38 | 32 |
| M2 | 31 | 40 | 43 | 31 |
| M3 | 36 | 33 | 41 | 38 |

Consider $\mathrm{m} / \mathrm{c}$ as treatment and worker as block. Apply ANOVA table at the level of 5\% Significance.

