PARUL UNIVERSITY
FACULTY OF ENGINEERING \& TECHNOLOGY
M.Tech. Winter 2017-18 Examination

## Semester: I

Subject Code: 03214102
Subject Name: Operation Research in Water Resources Engineering

Date: 28/12/2017
Time: 2:00pm-4:30pm
Total Marks: 60

## Instructions:

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Make suitable assumptions wherever necessary.
4. Start new question on new page.
Q.1(A) Discuss the necessity of operation research.
Q.1(B) How to formulate linear programming problem?
Q.1(C) Why sensitivity analysis is to be carried out?

## Q. 2 Answer the following questions. (Attempt any three)

Q. 2 (A) Express the following L P models into standard form :
i) Maximize $Z=6 X_{1}+2 X_{2}$
S.T. $\quad 2 \mathrm{X}_{1}+4 \mathrm{X}_{2} \leq 30$
$24 X_{1}+X_{2} \geq 3$
$\mathrm{X}_{1}, \mathrm{X}_{2} \geq 0$
ii) Minimize $Z=4 X_{1}+3 X_{2}+6 X_{3}$

S T $\quad X_{1}+2 X_{2}-3 X_{3} \leq 15$

$$
6 X_{1}-4 X_{2}+2 X_{3} \geq 15
$$

$$
8 X_{1}+2 X_{2}+4 X_{3}=-10
$$

$$
X_{1}, X_{2}, X_{3} \geq 0
$$

Q. 2 (B) Construct the dual of the problem Maximize $Z=3 X_{1}+10 X_{2}+2 X_{3}$ S T $\quad 2 \mathrm{X}_{1}+3 \mathrm{X}_{2}+2 \mathrm{X}_{3} \leq 7$

$$
\begin{aligned}
& 3 \mathrm{X}_{1}-2 \mathrm{X}_{2}+4 \mathrm{X}_{3}=3 \\
& \mathrm{X}_{1}, \mathrm{X}_{2}, \mathrm{X}_{3} \geq 0
\end{aligned}
$$

Q. 2 (C) The following matrix gives the payoff of different strategies $S_{1}, S_{2}$ and $S_{3}$ against the conditions $\mathrm{N}_{1}, \mathrm{~N}_{2}, \mathrm{~N}_{3}$ and $\mathrm{N}_{4}$. Determine the decision taken under Pessimistic approach.

|  | $\mathrm{N}_{1}$ | $\mathrm{~N}_{2}$ | $\mathrm{~N}_{3}$ | $\mathrm{~N}_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~S}_{1}$ | Rs 100,000 | Rs 50,000 | Rs $-20,000$ | Rs $-75,000$ |
| $\mathrm{~S}_{2}$ | Rs 50,000 | Rs 20,000 | Rs $-40,000$ | Rs $-60,000$ |
| $\mathrm{~S}_{3}$ | Rs 20,000 | Rs $-10,000$ | Rs $-15,000$ | Rs $-20,000$ |

Q. 2 (D) With reference to Q 2 (C) determine the decision taken under Regret approach .
Q. 3 (A) Find out the solution of the following linear programming problem graphically :

Minimize $\mathrm{Z}=20 \mathrm{X}_{1}+10 \mathrm{X}_{2}$

$$
\text { S T } \begin{aligned}
\mathrm{X}_{1}+2 \mathrm{X}_{2} & \leq 40 \\
3 \mathrm{X}_{1}+X_{2} & \geq 30 \\
4 \mathrm{X}_{1}+3 X_{2} & \geq 60 \\
X_{1}, X_{2} & \geq 0
\end{aligned}
$$

Q. 3 (B) Solve the Q 3 (A) analytically up to only two tableau.

Find out decision making under risk by expected value criteria using following data :
Q. 3 (B) Cost of a mobile is Rs 15,000 and selling price of the same is Rs 20,000 . There is no reason for a salesperson to by less than 10 and more than 15 mobiles per day. He cannot return unsold mobiles. How many mobiles she should order?

| No. of <br> mobiles <br> sold | Probability <br> $\%$ |
| :---: | :---: |
| 10 | 10 |
| 11 | 15 |
| 12 | 18 |
| 13 | 22 |
| 14 | 30 |
| 15 | 05 |

Q. 4 (A) Cadilla Pharmaceuticals Limited divided its marketing area into three zones. The amount of sales
depends up on the number of salesmen in each zone. The firm has been collecting the data regarding the sales and salesmen in each area over a number of years.
The information is summarized and given below. For the next year the firm has only 9 salesmen to three different zones so that the total sales are maximum.

| No. Of salesmen | Profits in lakhs <br> of Rs | Profits in lakhs <br> of Rs | Profits in <br> lakhs of Rs |
| :--- | :--- | :--- | :--- |
|  | Zone I | Zone II | Zone III |
| 0 | 3.0 | 3.5 | 4.2 |
| 1 | 4.5 | 4.5 | 5.4 |
| 2 | 6.0 | 5.2 | 6.0 |
| 3 | 7.0 | 6.4 | 7.0 |
| 4 | 7.9 | 7.2 | 8.2 |
| 5 | 9.0 | 8.2 | 9.5 |
| 6 | 9,8 | 9.3 | 10.2 |
| 7 | 10.5 | 9.8 | 11.0 |
| 8 | 10.0 | 10.0 | 11.0 |
| 9 | 9.0 | 10.0 | 11.0 |

## OR

Q. 4 (A) Determine an initial basic feasible solution to the following transportation problem using row minima method.

|  |  | To |  |  |  |  | Available, tonnes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ | $\mathrm{D}_{5}$ |  |
| From | $\mathrm{S}_{1}$ | $30 \mathrm{Rs} / \mathrm{t}$ | $40 \mathrm{Rs} / \mathrm{t}$ | $60 \mathrm{Rs} / \mathrm{t}$ | $80 \mathrm{Rs} / \mathrm{t}$ | $90 \mathrm{Rs} / \mathrm{t}$ | 20 |
|  | $\mathrm{S}_{2}$ | $20 \mathrm{Rs} / \mathrm{t}$ | $100 \mathrm{Rs} / \mathrm{t}$ | $10 \mathrm{Rs} / \mathrm{t}$ | $50 \mathrm{Rs} / \mathrm{t}$ | $80 \mathrm{Rs} / \mathrm{t}$ | 30 |
|  | $\mathrm{S}_{3}$ | $70 \mathrm{Rs} / \mathrm{t}$ | $110 \mathrm{Rs} / \mathrm{t}$ | $200 \mathrm{Rs} / \mathrm{t}$ | $400 \mathrm{Rs} / \mathrm{t}$ | $30 \mathrm{Rs} / \mathrm{t}$ | 15 |
|  | $\mathrm{S}_{4}$ | $20 \mathrm{Rs} / \mathrm{t}$ | $10 \mathrm{Rs} / \mathrm{t}$ | $90 \mathrm{Rs} / \mathrm{t}$ | $140 \mathrm{Rs} / \mathrm{t}$ | 160 Rs / t | 13 |
| Demand , tonnes |  | 40 | 6 | 8 | 18 | 6 |  |

Q. 4 (B) Solve Q 4 (A) i.e. above problem by VAM.

