

**PARUL UNIVERSITY**  
**FACULTY OF ENGINEERING & TECHNOLOGY**  
**M.Tech.Winter2018 – 19 Examination**

**Semester: 1**  
**Subject Code: 03209104**  
**Subject Name: Theory of Elasticity**

**Date: 12/12/2018**  
**Time: 10:30 am to 01:00 pm**  
**Total Marks: 60**

**Instructions:**

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Make suitable assumptions wherever necessary.
4. Start new question on new page.

Q.1 A) Mention the significance and applications of theory of elasticity? (05)

B) Write a comprehensive note on stress concentration. (05)

C) What is Cauchy's stress principle? Explain with mathematical expression. (05)

Q.2 Answer the following questions. (Attempt any three) (Each five mark) (15)

A) Write a short note on macroscopic behaviour of material

B) State and justify the basic assumptions in theory of elasticity.

C) The following are the principal stress at a point in a stressed material. Taking  $E=210\text{kN/mm}^2$  and  $\nu=0.3$ , calculate the volumetric strain and the Lamé's constants.

$$\sigma_x=200\text{N/mm}^2, \sigma_y=150\text{N/mm}^2, \sigma_z=120\text{N/mm}^2$$

D) Write a short note on following. (Mention the statement and Equation)

i. Tresca's criteria

ii. Von Mises criteria.

A) Is the following state of strain possible?

Q.3 
$$\begin{aligned} e_x &= A(x^2+y^2) & \gamma_{xy} &= 2Axy \\ e_z &= \gamma_{xz} = \gamma_{yz} = 0 & e_y &= Ay^2 \end{aligned} \quad (07)$$

B) The stress components at a point in a body are given by

$$\sigma_x=3xy^2+2x, \sigma_y=5xyz+3y, \sigma_z=x^2y+y^2z, \tau_{xy}=0, \tau_{yz}=\tau_{xz}=3xy^2+2xy$$

Determine whether these components of stress satisfy the equilibrium equations or not at the point (1,-1, 2). If not then find body force at this point so that the stress components are under equilibrium. (08)

**OR**

B) The state of strain at a point is given by:

$$\epsilon_x=0.001, \epsilon_y=-0.003, \epsilon_z=\gamma_{xy}=0, \gamma_{xz}=-0.004, \gamma_{yz}=0.001$$

Determine the stress tensor at this point. Take  $E = 210 \times 10^6 \text{kN/m}^2$ , Poisson's ratio = 0.28. Also find Lamé's constant. (08)

Q.4 A) Derive the relationship between plane stress and plane strain for plane stress case. (07)

**OR**

A) Derive the strain-strain relationship equation (Generalized Hooke's law) for linearly isotropic material. (07)

B) Derive expression for two dimensional stress at a point. Also, Derive expression for principle stress and principle plane for two dimensional stresses. (08)