

PARUL UNIVERSITY
FACULTY OF ENGINEERING & TECHNOLOGY
M. Tech. Winter 2019 - 20 Examination

Semester: 3

Subject Code: 203206231

Subject Name: Computation Method for Automobile Engineering

Date: 26/11/2019

Time: 10:30 am to 1 pm

Total Marks: 60

Instructions:

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Make suitable assumptions wherever necessary.
4. Start new question on new page.

- Q.1** A) What is Error? What are the different types of Error occurs in numerical methods? (05)
 B) Write short note on following MATLAB operation. (05)

I. Function File II. Script File

- C) Find root of equation $x^3 - 2x - 5 = 0$ by Regula- falsi method, correct to three decimal places. (05)

- Q.2** Answer the following questions. (Attempt any three) (15)

- A) If $\frac{dy}{dx} = x + yz$ and $\frac{dz}{dx} = x^2 - y^2$ use Runge - Kutta 4th order method under boundary condition $y(1)=1$ and $z=0.5$ find y and z at 1.2 take $h=0.1$

- B) If $\frac{dy}{dx} = 1 + y$ given $y(0)=0$ using Milne's predictor -corrector method find y at $x=0.5$ with step $h=0.1$ using following data

x	0	0.1	0.2	0.3
y	0	0.1051	0.2214	0.3498

- C) Give brief review of steps involved in pre-processor of finite element method.

- D) Develop the mathematical model for forced damped vibration.

- Q.3** A) Discuss about the stability analysis of Multi step method. (07)

- B) Solve the differential equation $\frac{dy}{dx} = \sqrt{x+y}$ using Modified Euler's method under the boundary $y(0)=0.36$ find $y(0.2)$ up to accuracy 0.0001 (08)

OR

- B) Solve $\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2}$ for the following condition using Crank Nicholson method. At $x=0$, and $x=3$, $u=0$ (08)
 for all values of 't'. At $t=0$, $u=x^2$ for $0 < x < 3$. Take increment in 'x' as '1' and increment in 't' as '0.1' find all values of 'u' at $t=0$ to $t=0.3$

- Q.4** A) A steel plate of $750 \times 750 \text{mm}$ has its two adjacent sides maintained at 100°C , while two other sides maintained at 0°C , what will be steady state temperature at interior points assuming a grid size of 250mm. (07)

OR

- A) solve the wave equation $\frac{\partial^2 u}{\partial x^2} - \frac{\partial^2 u}{\partial t^2} = 0$; $0 \leq x \leq 1$, $t \geq 0$ Subject to the following condition (07)

$u = x^2 + xt^2$, along the initial line $t = 0$ by using the method of characteristics, find the solution between the grid points $x = 0.1$ and $x = 0.2$

- B) Find the largest eigen value in modulus and the corresponding eigenvector of the matrix (08)

$$A = \begin{bmatrix} -15 & 4 & 3 \\ 10 & -12 & 6 \\ 20 & -4 & 2 \end{bmatrix}$$