

PARUL UNIVERSITY
FACULTY OF ENGINEERING & TECHNOLOGY
M.Tech. Winter 2019 - 20 Examination

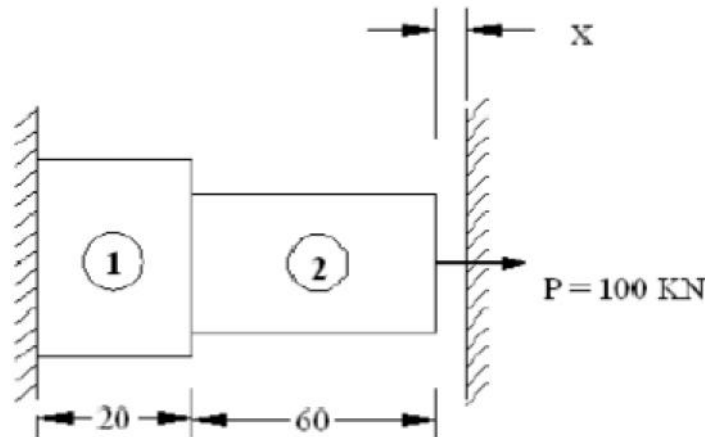
Semester: 1
Subject Code: 203219102
Subject Name: Finite Element Analysis in Design & Manufacturing

Date: 17/12/2019
Time: 10:30am to 1:00pm
Total Marks: 60

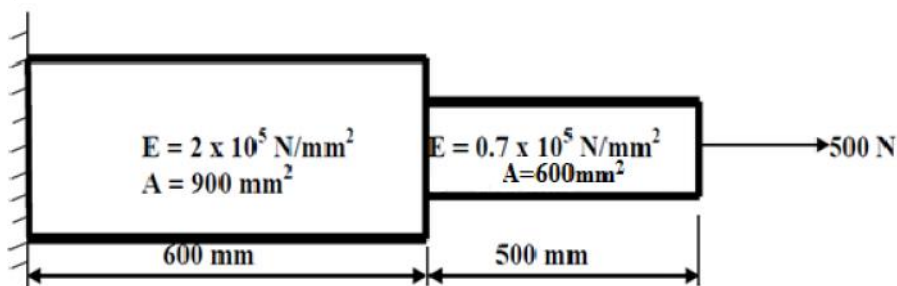
Instructions:

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Make suitable assumptions wherever necessary.
4. Start new question on new page.

- Q.1** A) Explain Penalty approach and Elimination approach for FEA. (05)
 B) State the applications of FEA in the field of engineering. (05)
 C) Explain the statement “FEM operates from part to the whole”. (05)
- Q.2** Answer the following questions. (Attempt any three) (15)
- A) Draw a sketch of following elements showing nodes:
 (i) Quadrilateral (ii) Six node triangular (iii) Tetrahedral
- B) What is shape function? Derive linear shape functions for 1-dimensional bar element in terms of natural coordinate.
- C) Discuss the assumptions taken in the derivation of stiffness matrix.
- D) Find the nodal displacements for the axially loaded stepped bar as shown in figure below using Penalty approach. $E=200\text{Gpa}$, $A_1= 200 \text{ mm}^2$, $A_2 =180 \text{ mm}^2$ and $x= 0.1 \text{ mm}$.

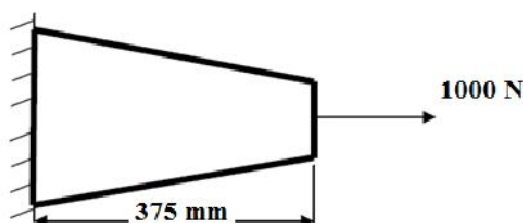


- Q.3** A) List and describe the general steps of the Finite Element Method. (07)
 B) Consider the stepped bar shown in figure below. Determine the Nodal Displacement, Stress in each element, Reaction forces.



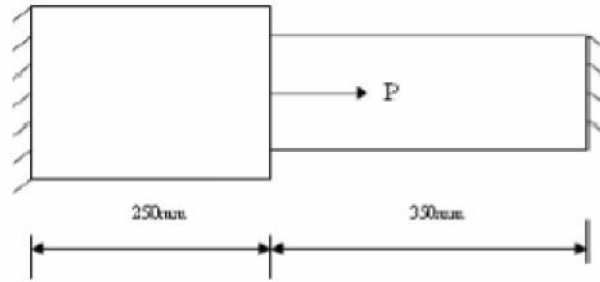
OR

- B) Consider the Tapered bar shown in figure. Determine the Nodal Displacement, Stress in each element, Reaction forces $E = 2 \times 10^5 \text{ N/mm}^2$, Area at root, $A_1 = 1000 \text{ mm}^2$, Area at the end, $A_2 = 500 \text{ mm}^2$.



A) A two-step bar as shown in Figure is subjected to thermal loading conditions. An axial load $P = 200 \times 10^3 \text{ N}$ applied 20° C to the end. The temperature of the bar is raised by 50° C . Consider $E_1 = 70 \times 10^3 \text{ N/mm}^2$, $E_2 = 200 \times 10^3 \text{ N/mm}^2$, $A_1 = 700\text{mm}^2$, $A_2 = 1000\text{mm}^2$, $\alpha_1 = 23 \times 10^{-6} \text{ per } ^\circ\text{C}$ and $\alpha_2 = 11.7 \times 10^{-6} \text{ per } ^\circ\text{C}$. Determine the Element stiffness matrix, Global stiffness matrix and force vector.

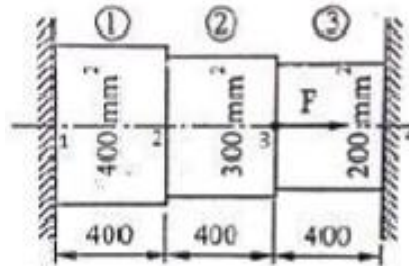
Q.4



(07)

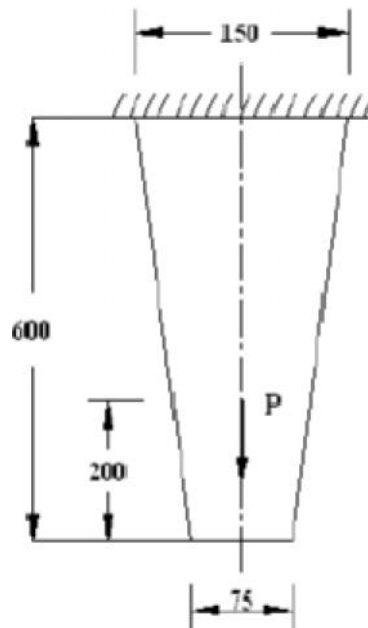
OR

A) Consider the bar shown in figure. An axial load $F=35 \text{ KN}$ is applied as shown. Using penalty approach for handling boundary conditions, determine nodal displacements and support reactions. Take $E=200 \text{ Gpa}$ for all elements. Length of each element is in mm.



(07)

B) A thin plate as shown in figure has a uniform thickness of 10 mm and modulus of elasticity is 200 Gpa. The plate is subjected to a point load $P = 500 \text{ N}$ as shown in figure. Model the problem with two elements and find stresses in each element.



(08)