## Instructions

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Make suitable assumptions wherever necessary.
4. Start new question on new page.

## Q. 1 Do as Directed.

A).Multiple choice type questions/Fill in the blanks. (Each of 1 mark)

1. If two variables are linearly independent then the correlation coefficient is $\qquad$
a) 0.5
b) 0
c) -1
d) +1
2. Total probability of happening an event and not happening an event is $\qquad$ -
a) 0
b) -1
c) 1
d) $1 / 2$
3. The mean and variance of Binomial Distribution is $\qquad$ and $\qquad$ .
a) $n p$ and $n p q$
c) ) nq and mq
b) 1 and 0
d) p and q
4. The correlation coefficient lies between $\qquad$ and $\qquad$ .
a) -1 and 1
b) -2 and 2
c) 0 and 1
d) -1 and 1
5. One of the regression coefficient of two perfectly correlated variables is 0.5 , hence the other regression coefficient is $\qquad$ -.
a) 0.5
b) -1
c) 1
d) 2
B).Define the following. (Each of 1 mark)
6. Mutually exclusive events
7. Random Variable
8. Probability Mass Function,
9. Correlation
10. Sample space
C).Direct questions. (Each of 1 mark)
1.Find the value of $E(3 x+2)$ where $E(x)=0.5$ ?
11. A and B are two independent events and $P(A)=\frac{1}{2}, P(B)=\frac{1}{5}$ find $P(A \cup B)$ ?
12. $\bar{X}$ and $R$ charts are based on which distribution.
13. Write difference between correlation and Regression?
14. Explain Conditional probability
Q. 2 Answer the following questions.
A).1). A group consists of seven men and some women. The probability of selecting two women from them is $\frac{1}{15}$. Find the number of women in the group.
2). A person tosses 3 coins simultaneously. He gets Rs. 8 if 3 heads appear, Rs. 4 if 2 heads appear and Rs. 2 if one head appears. What penalty should be charged if no head appears in order that game is fair?
B). 1) The Probability distribution of a random variable $x$ is as follows

| $x_{i}$ | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $P\left(x_{i}\right)$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{8}$ | $\frac{1}{8}$ |

Find the mean and variance of $x$.
2) If $A, B$ and $C$ are three mutually exclusive and exhaustive events and if
$3 P(A)=2 P(B)=6 P(C)$, find $P(A \cup B)$
Q. 3 Answer the following questions.
A).1) A bag contains 30 balls numbered 1 to 30 . One ball is drawn at random. Find the probability that the number of the ball drawn will be a multiple of (i) 5 or 7 and (ii) 3 or 7
2) For a Binomial distribution $\mathrm{n}=5$ and $P(x=1)=P(x=2)$, find $P(x=3)$.
B). 1) There are 100 misprints in a book of 100 pages. If a page is selected at random, find the probabilities that (i) there will be no misprint in the page (ii) there will be 1 misprint (iii) there will be at the most 2 misprints.
2) There are 10 electric bulbs in a box in which 3 are defective bulbs. If 3 bulbs are selected at random from the box, find the expected number of defective bulbs
Q. 4 Attempt any three questions. (Each of 5 mark)

1. Find the Karl Pearson's coefficient of correlation from the following data:

| $X$ | 100 | 101 | 102 | 102 | 100 | 99 | 97 | 98 | 96 | 95 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $Y$ | 98 | 9 | 99 | 97 | 95 | 92 | 95 | 94 | 90 | 91 |

2. Find the equations of regression line $Y$ on $X$ from the following data. Also find $Y$ when $X=45$.

| $X$ | 28 | 41 | 40 | 38 | 35 | 33 | 46 | 32 | 36 | 33 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $Y$ | 30 | 34 | 31 | 34 | 30 | 26 | 28 | 31 | 26 | 31 |

3. The following table gives the information regarding life hours of 5 fluorescent lamps of 10 different samples. Draw $\bar{X}$ and $R$ charts and state your conclusions. Also give the revised limits for the control of the future production.

| Sample <br> number | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\bar{X}$ | 3290 | 3180 | 3350 | 3370 | 3280 | 3240 | 3260 | 3410 | 3310 | 3510 |
| $R$ | 360 | 210 | 50 | 100 | 50 | 400 | 500 | 200 | 300 | 600 |

[For $\mathrm{n}=5, \mathrm{~A}_{2}=0.58, \mathrm{D}_{3}=0, \mathrm{D}_{4}=2.11$ ]
4. Assume that a factory has two machines. Past records show that machine A produces 305 of the items of output and machine B produces 705 of the items. Further, $5 \%$ of the items produced by machine A were defective and only $1 \%$ produced by machine B were defective. If a defective item is drawn at random, what is the probability that the defective item was produced by machine A or machine B ?

