

**PARUL UNIVERSITY**  
**FACULTY OF APPLIED SCIENCE**  
**M.Sc./IMSC, Winter 2019-20 Examination**

Semester: 1/7

Subject Code: 11204102

Subject Name: Classical Mechanics I &amp; Statistical Mechanics

Date: 02/12/2019

Time: 10:30 am to 01:00 pm

Total Marks: 60

**Instructions:**

1. All questions are compulsory.
2. Figures to the right indicate full marks.
3. Make suitable assumptions wherever necessary.
4. Start new question on new page.

**Q.1. A) Essay type/ Brief note (4x2) (Each of 04 marks) (08)**

- (a) Derive the Canonical transformation equation using the generating function  $F(q,Q,t)$  and  $F(q,P,t)$ .
- (b) Derive the canonical equation in term of Poisson bracket.

**Q.1. B) Answer the following questions (Any two)**

- (a) Short note/ Brief note (2x2)/ Schematically label the figures (2x2) (Each of 02 marks) (04)
  1. Define Poisson bracket
  2. Define eigen vector and eigen frequency.
- (b) Explain the separation of variable in the Hamilton Jacobi equation. (04)
- (c) Briefly explain the small oscillation of the particle on string. (04)

**Q.2. A) Answer the following questions.**

- (a) Short note/ Brief note (2x2)/ Fill in the blanks. (Each of 02 marks) (04)
  1. Write down the Hamiltonian equation of motion
  2. Write down the general case of coupled oscillation
- (b). Explain the application of Euler's angle in the heavy symmetric top. (04)

**Q.2. B) Answer the following questions (Any two)**

- (a) Short note/ Multiple choice questions. (Each of 01 marks) (03)
  1. Lagrangian  $L$  is:
 

(A) $L = \sum p\dot{q} - H$	(B) $L = \sum p\dot{q} + H$
(C) $L = \sum pq - H$	(D) $L = \sum p\dot{q}$
  2. For a transformation to be canonical, if:
 

(A) Poisson bracket changes sign	(B) Poisson bracket becomes zero
(C) Poisson bracket becomes unity	(D) Poisson bracket becomes invariant
  3. The normal coordinate  $x_K$  is
 

(A) $Ce^{i\omega t}$	(B) $Ce^{i\omega t}$	(C) $Ce^{i\omega t}$	(D) $Ce^{i\omega t}$
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- (b) Derive the expression of Hamilton Jacobi equation. (03)
- (c) Define and explain the Euler's angle. (03)

**Q.3. A) Essay type/ Brief note (4x2) (Each of 04 marks) (08)**

- (a) Explain the power spectrum of fluctuation and their correlation.
- (b) Explain the first order phase transition

**Q.3. B) Answer the following questions (Any two)**

- (a) Short note/ Brief note (2x2)/ Schematically label the figures (2x2) (Each of 02 marks) (04)
  1. Write down the statement of fluctuation-dissipation theorem.
  2. Draw a Phase transition diagram for water.
- (b) Explain the Brownian motion of particles. (04)
- (c) Describe the Vander Walls theory of liquid condensation. (04)

**Q.4. A) Answer the following questions.**

- (a) Short note/ Brief note (2x2)/ Fill in the blanks. (Each of 02 marks) (04)
  1. Fokker Planck equation is .....
  2. Clusius - Clayperon equation is.....
- (b) Describe the theory of Ising model. (04)

**Q.4. B) Answer the following questions (Any two)**

(a) Short note/ Multiple choice questions. (Each of 01 marks)

**(03)**

1. The Gibbs free energy is:

(A)  $G = H + TS$       (B)  $G = H - TS$       (C)  $G = TS$       (D) None of these

2. Latent heat is:

(A)  $T - S$       (B)  $T + S$       (C)  $T / S$       (D)  $T \cdot S$

3. Shot noise is related to:

(A) Sound vibration      (B) During the generation of waves  
(C) fluctuation due to discrete charge carriers      (D) None of these

(b) State and explain Wiener - Khinching theorem.

**(03)**

(c) Write down the condition of Phase equilibrium.

**(03)**