

Enrollment Number: _____

PARUL UNIVERSITY
FACULTY OF ENGINEERING & TECHNOLOGY
B. TECH MIDSEM EXAMINATION
3rd SEMESTER
ACY-2022-23 (ODD SEM)

Subject Name (Code): Discrete Mathematics(203191206)

Branch: CSE/IT

Date:09/08/2022

Time: 2:30PM to 4:00PM

Total Marks: 40

- | Sr.
No. | Marks |
|--|-------|
| Q.1 (A) One line Questions | 05 |
| 1 Truth value of $F \rightarrow T =$ _____. | |
| 2 $p \wedge p = p$ is known as _____ Law. | |
| 3 $n(A)=2$ And $n(B)=3$ then total number of non-trivial relations from A to B is _____ | |
| 4 If an algebraic structure satisfies associative and existence of identity property then it is known as _____. | |
| 5 State the Fundamental Theorem Of Arithmetic. | |
| Q.1 (B) Compulsory Question | 05 |
| 1 Identity relation on any set is always reflexive[true/false] | |
| 2 Subtraction is binary operation on \mathbb{N} . [true/false] | |
| 3 $\sqrt{31}$ is _____ number. | |
| 4 Euclidean algorithm is used to find _____ of two numbers. | |
| 5 If the relation is reflexive then diagonal entry s of Metrix representation must be _____ | |
| Q.2 Attempt any four (Short Questions) | 12 |
| 1 Determine whether the compound propositions is satisfiable or not
$(p \wedge q) \vee (\neg p \wedge \neg q)$ | |
| 2 $R=\{(1,1),(1,2),(2,1),(3,2)\}$ be the relation on $A=\{1,2,3\}$ then find Reflexive closure ,symmetric closure, And Transitive closure. | |
| 3 Write the converse ,inverse and contrapositive of the following statement
"If the weather is nice, then I'll wash the car." | |
| 4 Let R and S be relations on a set A represented by the matrices $M_R = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$ and
$M_S = \begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$. Find the matrices representing the following relations.
(a) $R \cup S$ (b) $R \cap S$ (c) $S \circ R$ (d) $R \circ S$ (e) $R \oplus S$ | |
| 5 Show that (\mathbb{Z}, \times) is monoid. | |
| Q.3 Attempt any two | 08 |
| 1 Check whether the (\mathbb{Z}, \geq) is partially ordered relation or Not. | |

2 By using the method of Contradiction show that $3+\sqrt{2}$ is irrational.

3 Using the concept of mathematical induction show that $1^3 + 2^3 + 3^3 + \dots + n^3 = \frac{(n(n+1))^2}{4}$

Q.4 a) Show that $((p \vee q) \wedge (\neg p \vee r)) \rightarrow (q \rightarrow r)$ is Tautology.

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b) Show that $(\mathbb{R}, +)$ is Abelian Group.

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OR

Let $A = \{1, 2, 3, 4\}$ and $R = \{(1, 2)(2, 4)(2, 2)(2, 3)(2, 3)(1, 1)(2, 1)(4, 2)\}$

05

- i) Draw the diagraph of the above relation
- ii) Write Matrix Representation Of above relation
- iii) Check that the relation is equivalence or not.